

---

# BERN-FRIBOURG GRADUATE SEMINAR

a seminar for Master and PhD students

---

Thursday 22<sup>nd</sup> February, 2024: 17:15 - 18:00

Room B7, Exakte Wissenschaften, Bern

MARTINA JØRGENSEN

ETH Zürich

## Injective hulls and higher rank hyperbolicity

### Abstract

We introduce the notions of asymptotic rank and injective hulls before investigating a coarse version of Dress'  $2(n+1)$ -inequality characterising metric spaces of combinatorial dimension at most  $n$ . This condition, referred to as  $(n, \delta)$ -hyperbolicity, reduces to Gromov's quadruple definition of  $\delta$ -hyperbolicity for  $n = 1$ . The  $\ell_\infty$  product of  $n$   $\delta$ -hyperbolic spaces is  $(n, \delta)$ -hyperbolic and, without further assumptions, any  $(n, \delta)$ -hyperbolic space admits a slim  $(n+1)$ -simplex property analogous to the slimness of quasi-geodesic triangles in Gromov hyperbolic spaces. Using tools from recent developments in geometric group theory, we look at some examples and show that every Helly group of asymptotic rank  $n$  acts geometrically on some  $(n, \delta)$ -hyperbolic space. Joint work with Urs Lang.